

# A potential transition from a concentrated to a generalized HIV epidemic the case of Madagascar

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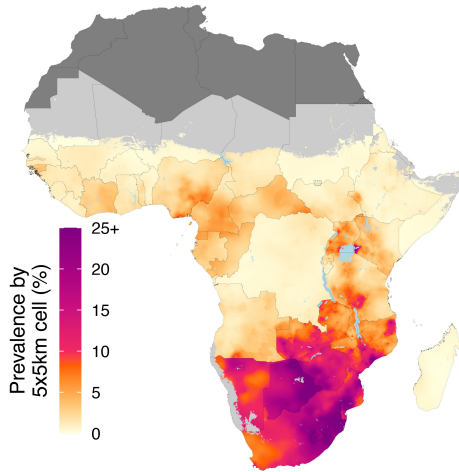
## Some facts

- 37.6 million [30.2 million–45.0 million] people globally were living with HIV in 2020.
- 1.5 million [1.1 million–2.1 million] people became newly infected with HIV in 2020.
- 690 000 [480 000–1 million] people died from AIDS-related illnesses in 2020.
- 77.5 million [54.6 million–110 million] people have become infected with HIV since the start of the epidemic
- 34.7 million [26.0 million–45.8 million] people have died from AIDS-related illnesses since the start of the epidemic.

Global HIV & AIDS statistics

<https://www.unaids.org/en/resources/fact-sheet>

- Why different countries and sub-regions show disparate HIV epidemic profiles?



## Data...

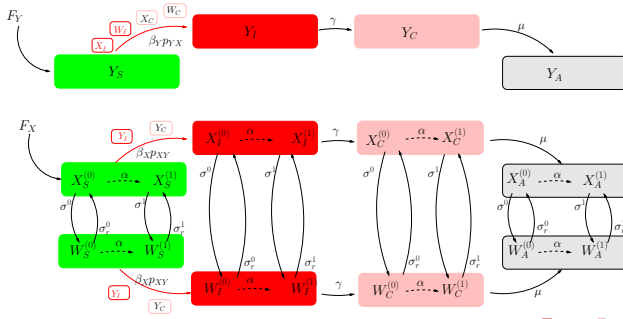
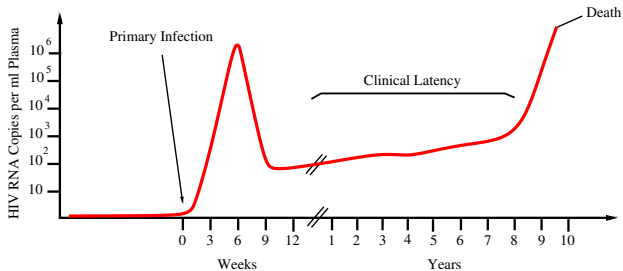
## 1 Little Data on Prevalence within SWs across main cities in Madagascar

|              | Sexual Worker Population |       |      |       | HIV Prevalence |      |      |      |      |      |
|--------------|--------------------------|-------|------|-------|----------------|------|------|------|------|------|
|              | 2014                     |       | 2017 |       | %              | 2012 | %    | 2016 |      |      |
|              | Min                      | Max   | Min  | Max   |                | CI   |      | CI   |      |      |
| Antananarivo | 28925                    | 35021 | 4908 | 12647 | 0.2            | 0.0  | 0.6  | 1.8  | 0.4  | 4    |
| Antsiranana  | 2978                     | 6812  | 4489 | 10749 | 0.0            | 0.0  | 0.0  | 2.9  | 0.8  | 6.5  |
| Mahajanga    | 2290                     | 5637  | 571  | 1516  | 3.0            | 0.8  | 6.2  | 22.7 | 13.9 | 31.2 |
| Toamasina    | 4289                     | 12336 | 3638 | 15120 | 1.8            | 0.2  | 3.9  | 5.4  | 2.9  | 8.1  |
| Fianarantsoa | 3415                     | 7795  | 743  | 2961  | 0.9            | 0.0  | 1.4  | 1.2  | 0.0  | 3.3  |
| Toliary      | 4190                     | 11367 | 1956 | 7530  | 1.2            | 0.0  | 3.9  | 2.7  | 0.7  | 5.1  |
| Taolagnaro   | 1392                     | 5059  | 830  | 2419  | 0.0            | 0.0  | 0.0  | 4.1  | 0.7  | 9.6  |
| Moramanga    | 1648                     | 2807  | 460  | 1388  | 0.3            | 0.0  | 0.5  | 0.6  | 0.0  | 5.7  |
| Antsirabe    | 3677                     | 9328  | 2150 | 6164  | 0.0            | 0.0  | 0.0  | 0.0  | 0.0  | 0.0  |
| Morondava    | 1648                     | 3672  | 502  | 1733  | 6.5            | 3.2  | 10.0 | 7.0  | 3.2  | 11.3 |
| Nosy Be      | 7268                     | 14830 | 2029 | 4048  | —              | —    | —    | 9.5  | 4.5  | 15.3 |

Data after the Institut National de la Statistique, Antananarivo, at 2018

## 2 Demographic data (detailed life tables from 2000)

Data from several public sources (WHO, CIA, Worldometers)



## Sexual encounters...

$$\begin{array}{ccc}
 Y_S + X_I^{(0)} & \xrightarrow{\beta_{YX} p_{YX} \textcolor{red}{X} f_0 f_X} & Y_I + X_I^{(0)} \\
 Y_S + X_I^{(1)} & \xrightarrow{\beta_{YX} p_{YX} \textcolor{red}{X} f_1 f_X} & Y_I + X_I^{(1)} \\
 Y_S + X_C^{(0)} & \xrightarrow{\beta_{YX} p_{YX} f_0 f_X} & Y_I + X_C^{(0)} \\
 Y_S + X_C^{(1)} & \xrightarrow{\beta_{YX} p_{YX} f_1 f_X} & Y_I + X_C^{(1)} \\
 Y_S + W_I^{(0)} & \xrightarrow{\beta_{YX} p_{YX} \textcolor{red}{X} f_0 f_W} & Y_I + W_I^{(0)} \\
 Y_S + W_I^{(1)} & \xrightarrow{\beta_{YX} p_{YX} \textcolor{red}{X} f_1 f_W} & Y_I + W_I^{(1)} \\
 Y_S + W_C^{(0)} & \xrightarrow{\beta_{YX} p_{YX} f_0 f_W} & Y_I + W_C^{(0)} \\
 Y_S + W_C^{(1)} & \xrightarrow{\beta_{YX} p_{YX} f_1 f_W} & Y_I + W_C^{(1)}
 \end{array}$$

$$\frac{dY_S}{dt} = F_Y - \beta_Y p_{YX} x Y_S - \delta Y_S$$

$$\frac{dY_I}{dt} = \beta_Y p_{YX} x Y_S - \delta Y_I - \gamma Y_I$$

$$\frac{dY_C}{dt} = \gamma Y_I - \mu Y_C - \delta Y_C$$

$$\frac{dY_A}{dt} = \mu Y_C - (1 + m) \delta Y_A$$

$$x = f_0 x_0 + (1 - f_0) x_1$$

$$x_0 = \frac{f_W (\chi W_I^{(0)} + W_C^{(0)}) + (1 - f_W)(\chi X_I^{(0)} + X_C^{(0)})}{N_f}$$

$$x_1 = \frac{f_W (\chi W_I^{(1)} + W_C^{(1)}) + (1 - f_W)(\chi X_I^{(1)} + X_C^{(1)})}{N_f}$$

$$\frac{dX_S^{(1)}}{dt} = -\beta_X p_{XY} y X_S^{(1)} - \delta X_S^{(1)} + \alpha X_S^{(0)} - \sigma^1 X_S^{(1)} + \sigma_r^1 W_S^{(1)}$$

$$\frac{dX_I^{(1)}}{dt} = \beta_X p_{XY} y X_S^{(1)} - \delta X_I^{(1)} + \alpha X_I^{(0)} - \gamma X_I^{(0)} - \sigma^1 X_I^{(1)} + \sigma_r^1 W_I^{(1)}$$

$$\frac{dX_C^{(1)}}{dt} = \gamma X_I^{(1)} - \mu X_C^{(1)} - \delta X_C^{(1)} + \alpha X_C^{(0)} - \sigma^1 X_C^{(1)} + \sigma_r^1 W_C^{(1)}$$

$$\frac{dX_A^{(1)}}{dt} = \mu X_C^{(1)} - (1 + m) \delta X_A^{(1)} + \alpha X_A^{(0)} - \sigma^1 X_A^{(1)} + \sigma_r^1 W_A^{(1)}$$

$$y = \frac{\chi Y_I + Y_C}{N_m}$$



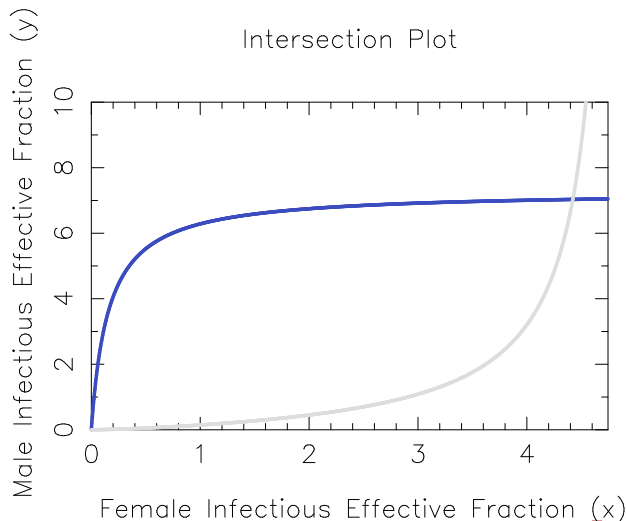
| Model Parameter                                      | Symbol                  | $V_0$ | $V_1$          | Refs.     |
|------------------------------------------------------|-------------------------|-------|----------------|-----------|
| Demographic parameters                               |                         |       |                |           |
| Recruitment rate into active sexual age              | $F_Y$                   | 0.00  | $5 \cdot 10^4$ | [8]       |
| Recruitment rate into active sexual age              | $F_X$                   | 0.00  | $5 \cdot 10^4$ | [8]       |
| Natural mortality percapita rate (X)                 | $\delta_X$              | 0.01  | 0.05           | [8]       |
| Natural mortality percapita rate (Y)                 | $\delta_Y$              | 0.01  | 0.05           | [8]       |
| Aging rate into the AF stage                         | $\alpha$                | 0.08  | 0.12           |           |
| Transition rate into the SW stage (YF)               | $\sigma^0$              | 0.00  | 0.05           |           |
| Reverse rate from the SW stage (YF)                  | $\sigma^0_{\downarrow}$ | 0.00  | 0.05           |           |
| Transition rate into the SW stage (AF)               | $\sigma^1$              | 0.00  | 0.05           |           |
| Reverse rate from the SW stage (AF)                  | $\sigma^1_{\downarrow}$ | 0.00  | 0.05           |           |
| Disease transmission parameters                      |                         |       |                |           |
| Total male sexual contact rate                       | $\beta_Y$               | 96.0  | 120.0          | [7]       |
| Total female sexual contact rate                     | $\beta_X$               | 96.0  | 120.0          | [7]       |
| Sexual worker $\beta_X$ factor $[(1 + \eta)\beta_X]$ | $\eta$                  | 0.00  | 19.00          |           |
| Male-to-Female transmission probability              | $p_{XY}$                | 0.00  | 0.005          | [7, 5, 4] |
| Female-to-Male transmission probability              | $p_{YX}$                | 0.00  | 0.001          | [7, 5, 4] |
| Transition rate from $I$ into $C$ stage              | $\gamma$                | 0.5   | 6.00           | [3]       |
| Transition rate from $C$ into $A$ stage              | $\mu$                   | 0.05  | 0.20           | [1]       |
| Disease-induced mortality factor $[(1 + m)\delta]$   | $m$                     | 0.00  | 99.00          |           |
| Infectious phase ( $I$ ) transmission factor         | $\chi$                  | 1.00  | 100.00         | [6]       |
| Male sexual preference factor (for SW)               | $f_W$                   | 0.00  | 0.99           |           |
| Male sexual preference factor (for YF)               | $f_0$                   | 0.00  | 0.99           |           |

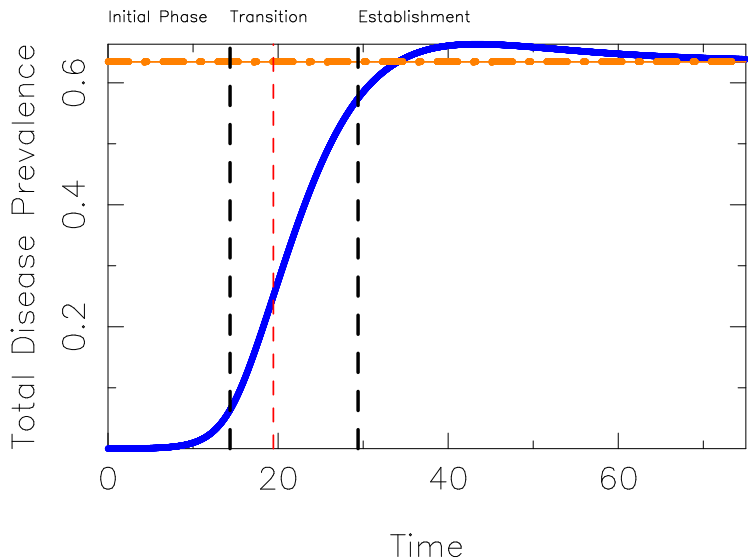
**Table 1:** Model Parameters for the *SICA* model.  $V_0$  and  $V_1$  define reasonable parameter ranges for each parameter value. Subscripts X and Y stand for female and male, respectively. YF, young female; AF, adult female; SW, sexual worker. All rates are given in year<sup>-1</sup>. Mortality and recruitment rates are directly estimated from life table information. Transmission probabilities are given per coital act and represent basal values. The  $\chi$  factor controls how much these are incremented when a healthy individual has a sexual encounter with an individual in the acute infection phase ( $I$ ).

| Model Parameter                                      | Symbol                  | $V_0$ | $V_1$          | Refs.     |
|------------------------------------------------------|-------------------------|-------|----------------|-----------|
| Demographic parameters                               |                         |       |                |           |
| Recruitment rate into active sexual age              | $F_Y$                   | 0.00  | $5 \cdot 10^4$ | [8]       |
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| Natural mortality percapita rate (X)                 | $\delta_X$              | 0.01  | 0.05           | [8]       |
| Natural mortality percapita rate (Y)                 | $\delta_Y$              | 0.01  | 0.05           | [8]       |
| Aging rate into the AF stage                         | $\alpha$                | 0.08  | 0.12           |           |
| Transition rate into the SW stage (YF)               | $\sigma^0$              | 0.00  | 0.05           |           |
| Reverse rate from the SW stage (YF)                  | $\sigma^0_{\downarrow}$ | 0.00  | 0.05           |           |
| Transition rate into the SW stage (AF)               | $\sigma^1$              | 0.00  | 0.05           |           |
| Reverse rate from the SW stage (AF)                  | $\sigma^1_{\downarrow}$ | 0.00  | 0.05           |           |
| Disease transmission parameters                      |                         |       |                |           |
| Total male sexual contact rate                       | $\beta_Y$               | 96.0  | 120.0          | [7]       |
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| Male-to-Female transmission probability              | $p_{XY}$                | 0.00  | 0.005          | [7, 5, 4] |
| Female-to-Male transmission probability              | $p_{YX}$                | 0.00  | 0.001          | [7, 5, 4] |
| Transition rate from $I$ into $C$ stage              | $\gamma$                | 0.5   | 6.00           | [3]       |
| Transition rate from $C$ into $A$ stage              | $\mu$                   | 0.05  | 0.20           | [1]       |
| Disease-induced mortality factor $[(1 + m)\delta]$   | $m$                     | 0.00  | 99.00          |           |
| Infectious phase ( $I$ ) transmission factor         | $\chi$                  | 1.00  | 100.00         | [6]       |
| Male sexual preference factor (for SW)               | $f_W$                   | 0.00  | 0.99           |           |
| Male sexual preference factor (for YF)               | $f_0$                   | 0.00  | 0.99           |           |

**Table 2:** Model Parameters for the *SICA* model.  $V_0$  and  $V_1$  define reasonable parameter ranges for each parameter value. Subscripts X and Y stand for female and male, respectively. YF, young female; AF, adult female; SW, sexual worker. All rates are given in year<sup>-1</sup>. Mortality and recruitment rates are directly estimated from life table information. Transmission probabilities are given per coital act and represent basal values. The  $\chi$  factor controls how much these are incremented when a healthy individual has a sexual encounter with an individual in the acute infection phase ( $I$ ).

## Some model analysis...

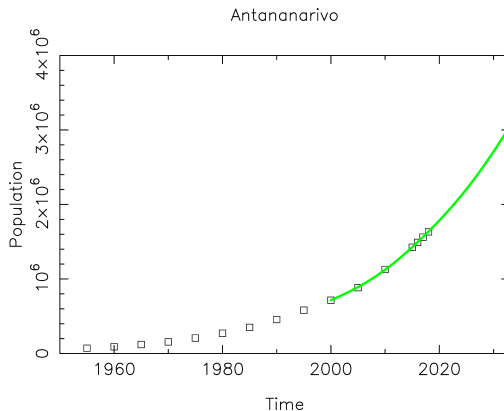




$$\begin{aligned}
 \frac{dY}{dt} &= F_Y - \delta_Y Y \\
 \frac{dX^{(0)}}{dt} &= F_X - \sigma^0 X^{(0)} + \sigma_r^0 W^{(0)} - \alpha X^{(0)} - \delta_X X^{(0)} \\
 \frac{dW^{(0)}}{dt} &= \sigma^0 X^{(0)} - \sigma_r^0 W^{(0)} - \alpha W^{(0)} - \delta_X W^{(0)} \\
 \frac{dX^{(1)}}{dt} &= \alpha X^{(0)} + \sigma_r^0 W^{(1)} - \sigma^0 X^{(1)} - \delta_X X^{(1)} \\
 \frac{dW^{(1)}}{dt} &= \alpha W^{(0)} + \sigma^0 X^{(1)} - \sigma_r^0 W^{(1)} - \delta_X W^{(1)}
 \end{aligned} \tag{1}$$

Further simplification...

$$\begin{aligned}
 \frac{dY}{dt} &= F_Y - \delta_Y Y \\
 \frac{dX}{dt} &= F_X - \delta_X X
 \end{aligned} \tag{2}$$



**Figure 1:** Demographic trends in Antananarivo. Solid green line: the numerical integration of the demographic model taking the population in 2000 as the initial condition, and time-dependent parameters  $F_Y$ ,  $F_X$ ,  $\delta_X$ ,  $\delta_Y$ , all estimated from life table data (2000-2016). Squares represent population data.

Source: <http://www.worldometers.info/world-population/madagascar-population/>

The  $R_0$ , the reproductive number...

The NGM [2] can be reduced to:

$$\mathbf{K} = \begin{bmatrix} 0 & k_{(1,3)} & k_{(1,4)} & k_{(1,5)} & k_{(1,6)} \\ k_{(3,1)} & 0 & 0 & 0 & 0 \\ k_{(4,1)} & 0 & 0 & 0 & 0 \\ k_{(5,1)} & 0 & 0 & 0 & 0 \\ k_{(6,1)} & 0 & 0 & 0 & 0 \end{bmatrix}$$

The characteristic equation thus reads:

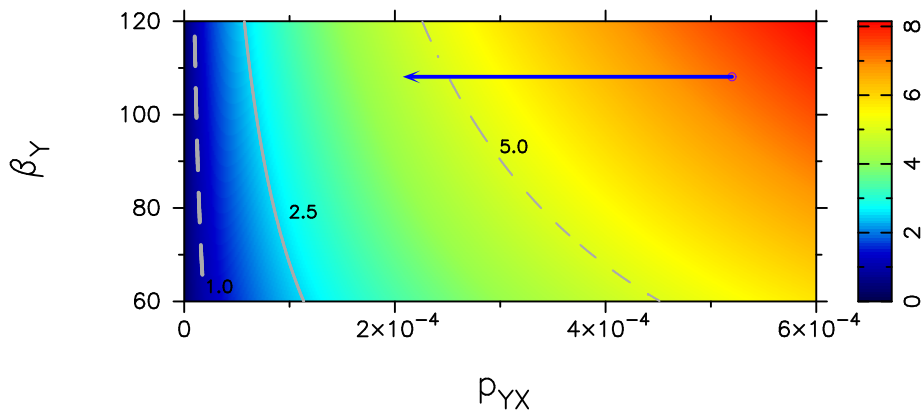
$$\det(\mathbf{K} - \lambda \mathbf{I}) = -\lambda^3 (\lambda^2 - \mathbf{k}_{(1,3)}\mathbf{k}_{(3,1)} - \mathbf{k}_{(1,4)}\mathbf{k}_{(4,1)} - \mathbf{k}_{(1,5)}\mathbf{k}_{(5,1)} - \mathbf{k}_{(1,6)}\mathbf{k}_{(6,1)})$$

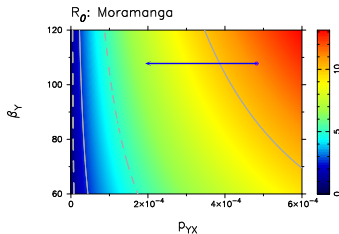
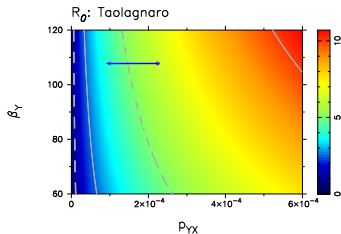
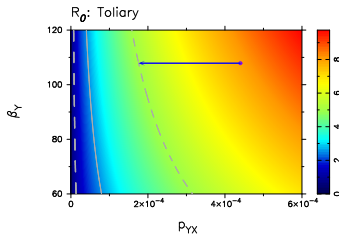
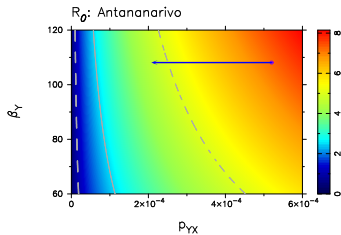
which leads to a final closed expression for  $R_0$ :

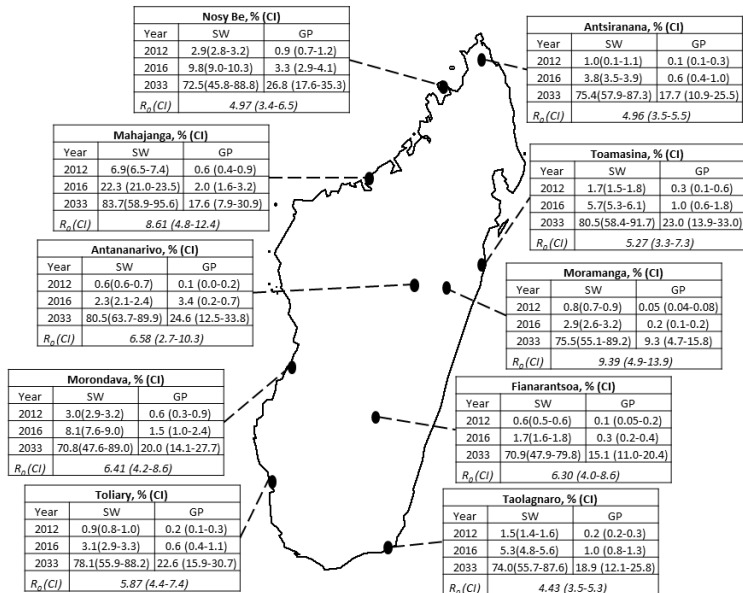
$$R_0 = \sqrt{k_{(1,3)}k_{(3,1)} + k_{(1,4)}k_{(4,1)} + k_{(1,5)}k_{(5,1)} + k_{(1,6)}k_{(6,1)}}$$

|                                 | Toliary             | Taolagnaro          | Moramanga           |
|---------------------------------|---------------------|---------------------|---------------------|
| Disease transmission parameters |                     |                     |                     |
| $\beta_Y$                       | $108.282 \pm 6.935$ | $107.897 \pm 6.775$ | $108.158 \pm 6.738$ |
| $\beta_X$                       | $108.308 \pm 6.955$ | $108.342 \pm 6.871$ | $107.776 \pm 6.900$ |
| $\eta$                          | $6.248 \pm 4.875$   | $10.788 \pm 4.389$  | $14.804 \pm 2.887$  |
| $m_\delta$                      | $50.306 \pm 28.286$ | $46.779 \pm 29.143$ | $50.387 \pm 28.043$ |
| $f_W$                           | $0.498 \pm 0.221$   | $0.400 \pm 0.187$   | $0.521 \pm 0.237$   |
| $f_0$                           | $0.522 \pm 0.260$   | $0.509 \pm 0.273$   | $0.804 \pm 0.182$   |
| $p_{XY}$                        | $0.003 \pm 0.001$   | $0.003 \pm 0.001$   | $0.003 \pm 0.001$   |
| $p_{YX}$                        | $0.001 \pm 0.000$   | $0.000 \pm 0.000$   | $0.000 \pm 0.000$   |
| $\gamma$                        | $1.882 \pm 1.005$   | $2.415 \pm 0.955$   | $3.159 \pm 0.564$   |
| $\mu$                           | $0.098 \pm 0.050$   | $0.105 \pm 0.051$   | $0.133 \pm 0.051$   |
| $\chi$                          | $35.894 \pm 24.942$ | $49.076 \pm 23.731$ | $72.181 \pm 18.285$ |
| $R_0$                           | $5.110 \pm 1.878$   | $4.161 \pm 0.841$   | $7.323 \pm 2.291$   |

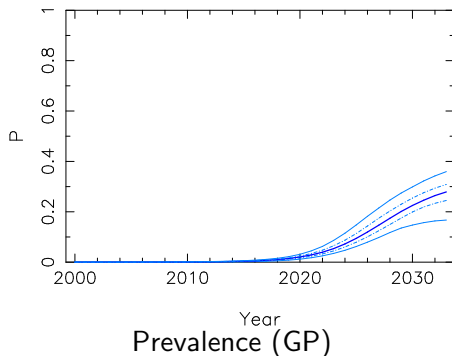
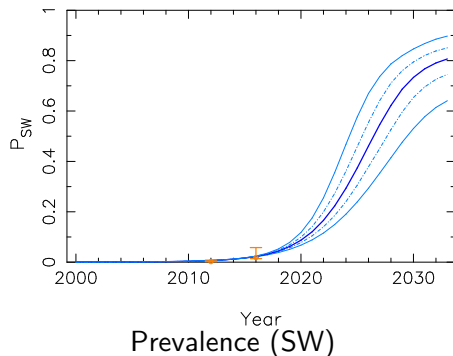


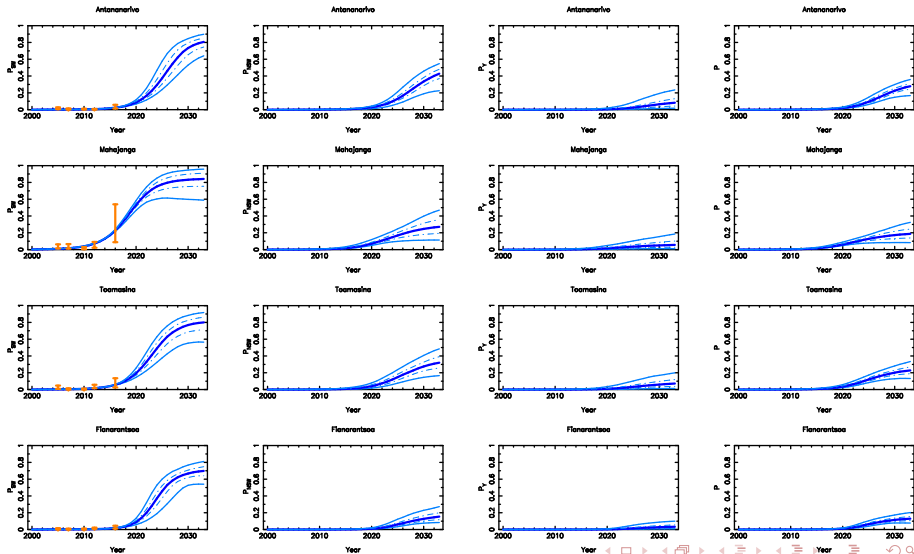
$R_0$ : Antananarivo





## Model Projections (Antananarivo)





- ❶ Our approach allows for HIV prevalence projections up to year 2033 across most important cities in Madagascar.
- ❷ Estimated  $R_0$  across cities in 2000, when incidence was extremely low, lies within real-life estimations reported for HIV (between 4 and 9).
- ❸ Our model consistently predicts sigmoid-like prevalence curves (with turning points within years 2020-2022) that reach a stable prevalence of HIV infection by 2033, within 9 to 24 percent in certain/most cities, similar to other high-prevalence regions in Southern Africa.
- ❹ Our results suggest that the late/delayed transition in Madagascar may have been due late introduction of HIV.
- ❺ Madagascar may be currently undergoing a transition from a concentrated to a generalized HIV epidemic, where young women would play a central key role
- ❻ A complex interplay between cultural (i.e., widespread practice of circumcision and women social vulnerability) and geopolitics (geographical and political population isolation) play a major role in determining the transition

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- [3] E. W. Fiebig, D. J. Wright, B. D. Rawal, P. E. Garrett, R. T. Schumacher, L. Peddada, C. Heldebrant, R. Smith, A. Conrad, S. H. Kleinman, and M. P. Busch. Dynamics of HIV viremia and antibody seroconversion in plasma donors: Implications for diagnosis and staging of primary HIV infection. *Aids*, 17(13):1871–1879, 2003.
- [4] R. H. Gray, M. J. Wawer, R. Brookmeyer, N. K. Sewankambo, D. Serwadda, F. Wabwire-Mangen, T. Lutalo, X. Li, T. VanCott, and T. C. Quinn. Probability of HIV-1 transmission per coital act in monogamous, heterosexual, HIV-1-discordant couples in Rakai, Uganda. *Lancet*, 357(9263):1149–1153, 2001.

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- [6] S. D. Pinkerton. Probability of HIV transmission during acute infection in Rakai, Uganda. *AIDS and Behavior*, 12(5):677–684, 2008.
- [7] M. J. Wawer, R. H. Gray, N. K. Sewankambo, D. Serwadda, X. Li, O. Laeyendecker, N. Kiwanuka, G. Kigozi, M. Kiddugavu, T. Lutalo, F. Nalugoda, F. Wabwire-Mangen, M. P. Meehan, and T. C. Quinn. Rates of HIV-1 transmission per coital act, by stage of HIV-1 infection, in Rakai, Uganda. *Journal of Infectious Diseases*, 191(9):1403–1409, 2005.
- [8] WHO. World Health Organization. global health observatory data repository. <http://apps.who.int/gho/data/node.home>, 2018. Accessed: 2018.02.01.



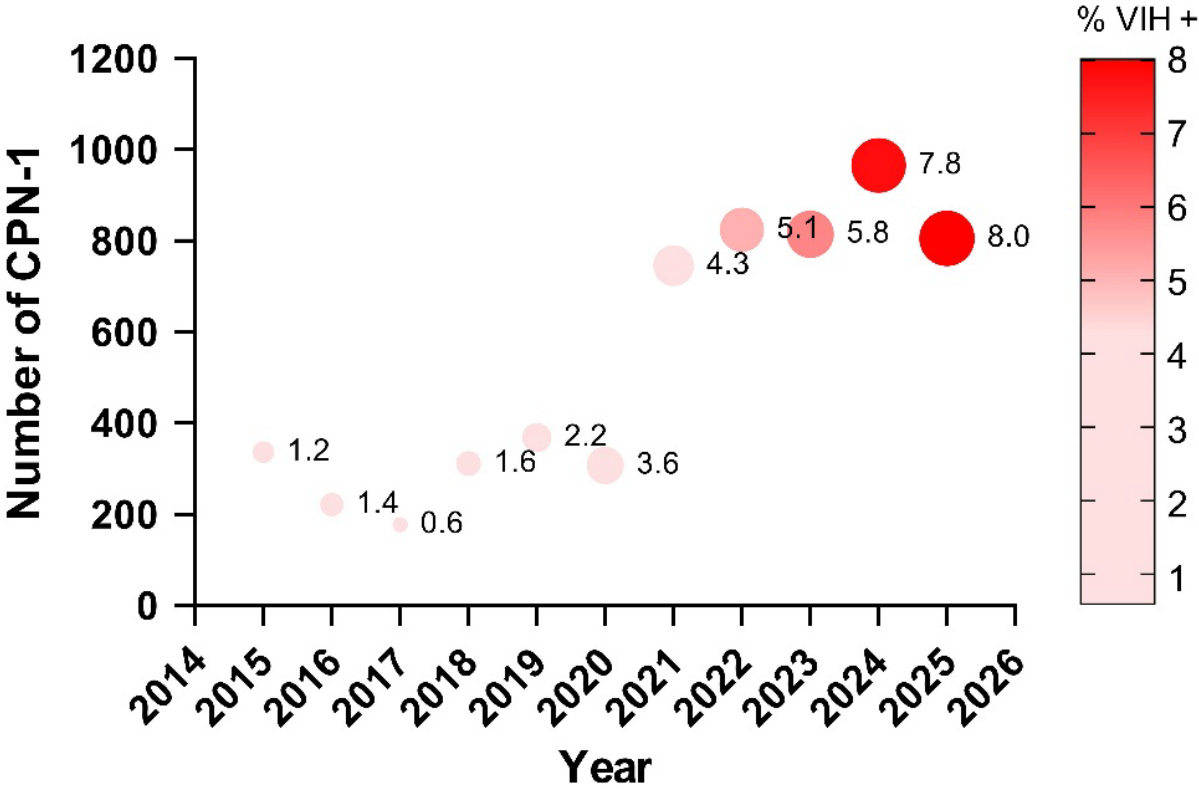


*Thank You So Much!*

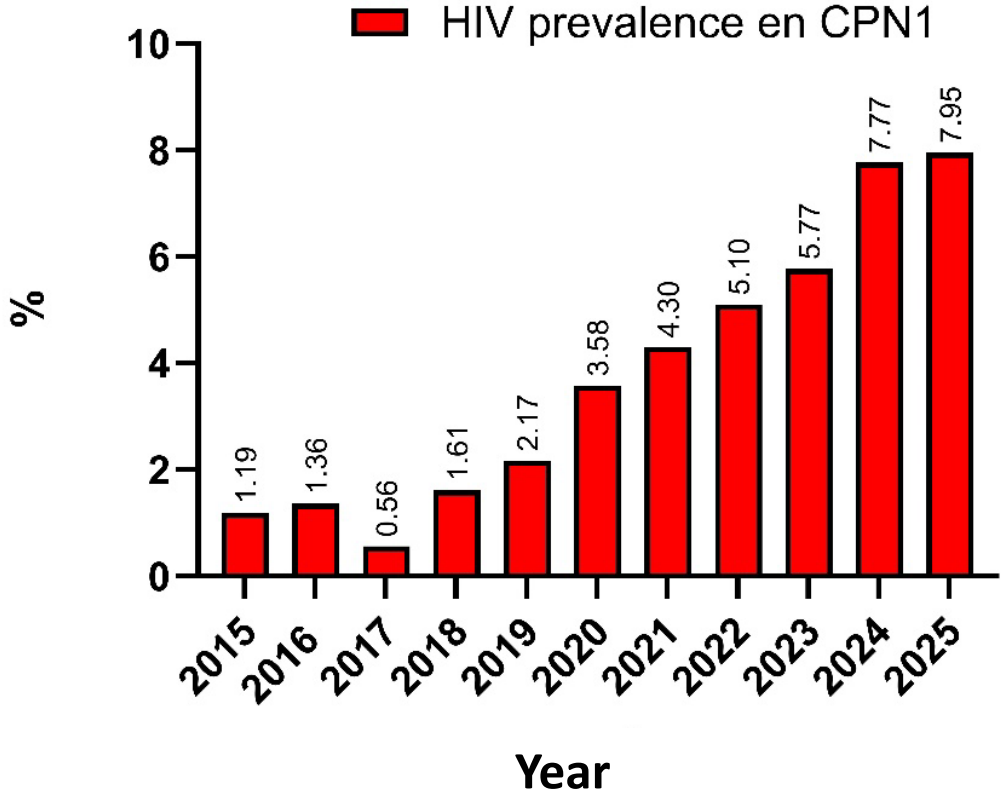
# Impact

- The modelling exercise has been a catalizer for the creation a working HIV group in Madagascar encompassing local and International NGO's, local Health authorities and local and International research institutions
- This group aims to coordinate and implement research initiatives and interventions to better ascertain the epidemiology of HIV in Madagascar and reinforce the response to the epidemic
- Actually, the results of the modelling study have been disseminated among local and International stakeholders and fòrums to raise the attention among this emerging Public Health threath in Madagascar

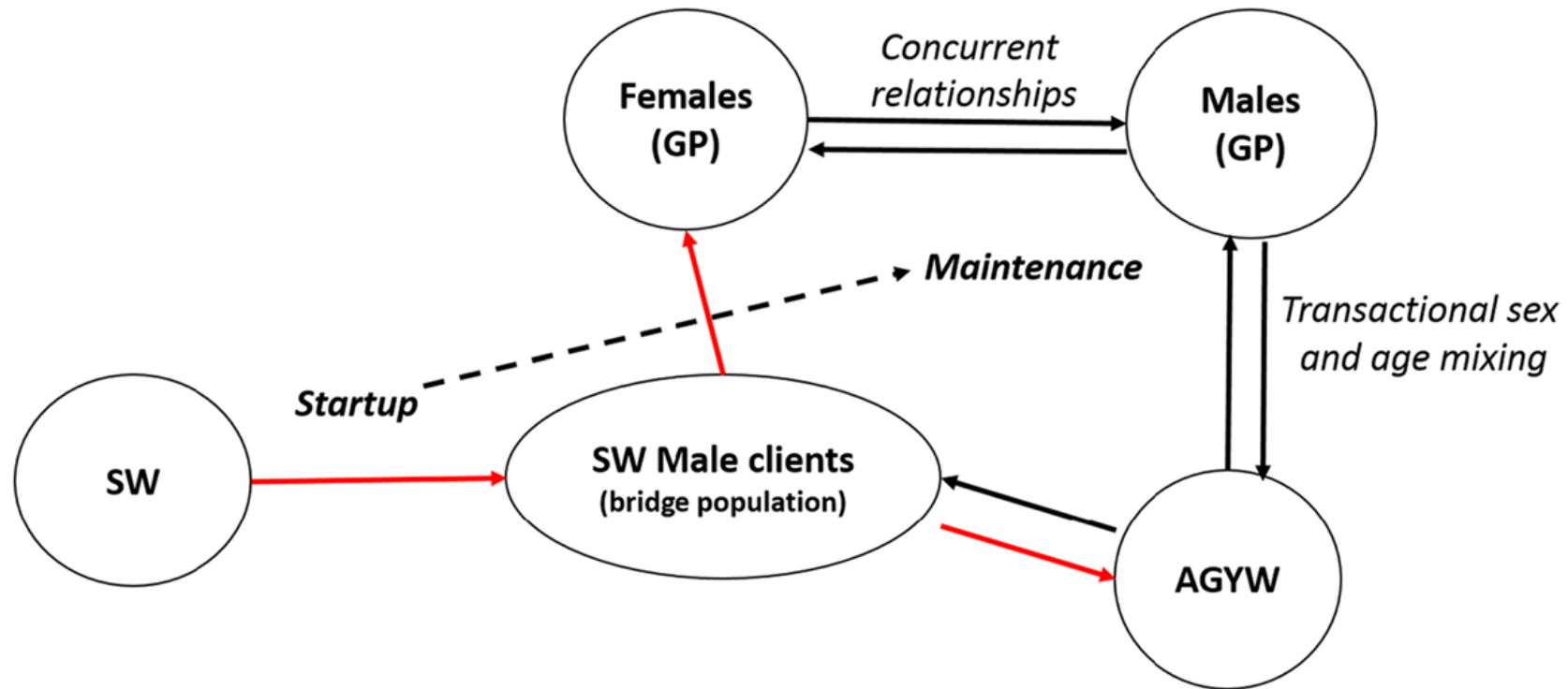
Positivity rate trend among pregnant women  
in the northern District of Ambanja  
(Madagascar)



Median age at diagnostic 23-24 years, range 14-42



# Conceptual framework of HIV epidemic generalisation



# Background and justification

- Very weak epidemiological surveillance
- Limited response to HIV epidemic: 20% HIV coverage of HIV testing among pregnant women, 30% coverage of ARV, etc.
- Response mainly focused to Key Populations, which have high prevalence of HIV
- Uncertain prevalence of HIV among General Population but presence of alarm signs of progression (i.e. Increasing TB-HIV coinfection, late diagnostics of Advanced AIDS disease among young people, fragmentary empirical data, etc.
- Widespread presence of all risk factors associated to HIV diffusion (i.e. Age mixing, population mobility transactional sex, multi-partner, inconsistent use of condoms, etc.)

## Is Madagascar at the edge of a generalised HIV epidemic? Situational analysis

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# Some empirical data

